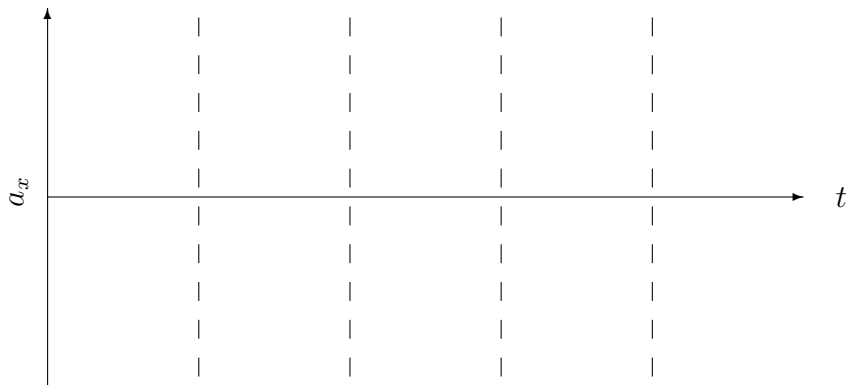
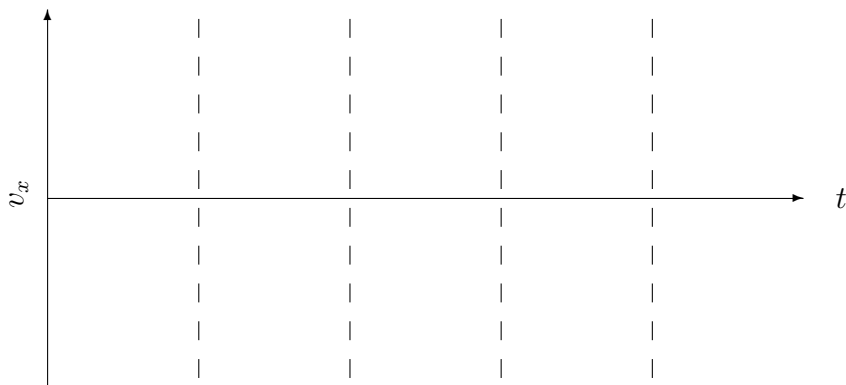
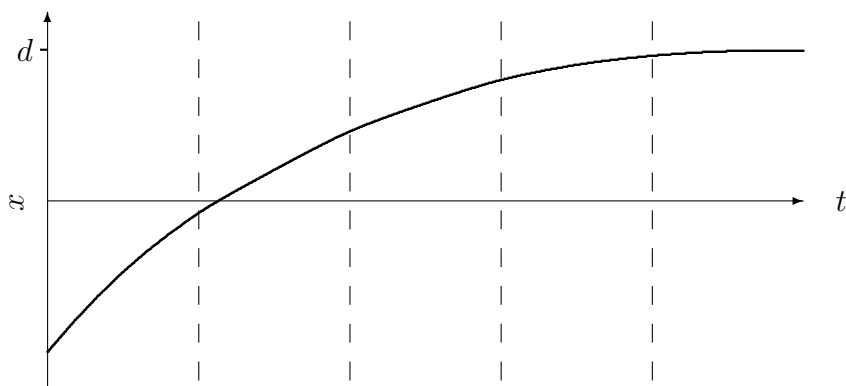


**Note:** You can ask me for help; for example, have me check if an answer is correct. Talk to me: you'll learn some physics, and that's the point of the course.

**1. (10 points)** The top graph displays how position depends on time for an object that gradually, but ever more slowly, approaches  $x = d$ . Make a qualitative sketch of the corresponding velocity versus time and acceleration versus time graphs for this motion.



**2. (30 points)** The distance from London to Sydney is  $1.70 \times 10^7$  m. You take a supersonic flight that covers this distance in exactly  $T = 2.00$  hours. Say the flight takes a time  $t_a$  to accelerate from rest, reaching a constant cruising speed of  $v_c$ , and then while landing, takes the same time  $t_a$  to decelerate. For a commercial flight that will be taken by people with varying health conditions, the magnitude of the horizontal component of the acceleration imposed on the passengers should not exceed  $2g$  ( $g = 9.80$  m/s<sup>2</sup>) for longer than three minutes. Calculate  $t_a$  for this maximum  $a_x = 2g$ , and determine whether this flight can be safe.



**3. (30 points)** You have a cannon that launches rubber balls with an initial speed of  $v_i = 12.6$  m/s. You set it at an angle  $\theta = 38^\circ$  above the horizontal, and shoot a ball at a high vertical wall standing a distance  $l = 9.20$  m in front of the cannon.

- (a) Find symbolic expressions for  $v_{fx}$  and  $v_{fy}$  at the instant before the rubber ball hits the wall. Then plug in the numbers and find their values.

- (b) The instant *after* the rubber ball bounces off the wall, the  $y$ -component of its velocity remains the same as it was just before it hit the wall. But the  $x$ -component of its velocity reverses its direction (same magnitude, opposite sign). Find out where, relative to the cannon, the ball falls back to the ground.

**4. (30 points)** You launch a projectile on a level surface on a planet with acceleration due to gravity  $g$ , starting from  $x_i = y_i = 0$ , with initial speed  $v_i$  and angle  $\theta$  with the  $x$ -axis. But you're facing a strong horizontal wind, so that the motion has a non-zero  $a_x = -w$ , where  $w$  is a positive constant that stands for the magnitude of the acceleration due to the wind.

(a) Write down the equations for motion along the  $x$  and  $y$ -axes:

$$v_{fx} = \qquad \qquad \qquad x_f =$$

$$v_{fy} = \qquad \qquad \qquad y_f =$$

(b) Find the *range* of the projectile: an equation for how far it will travel until it hits the ground again.

(c) Check your result: when you set  $w = 0$ , you should get the same equation for the range as you have in your class notes.

(d) The range is positive when  $w < [\text{an expression involving } g \text{ and } \theta]$ . Find this inequality. Would it make physical sense for the range to be negative?

(e) See what happens when  $w = g$  and  $\theta = 45^\circ$ . Interpret your result in this case—what does the motion look like?